

Thermoelectric Application Of Metal Telluride Nanostructures And Their Heterostructures

Mohammed Istafaul Haque Ansari¹, A. Y. Bokhary², Nafis Ahmad³

¹Department of Mechanical Engineering, Indian Institute of Technology Kanpur, Kanpur-208016, India

²Department of Mechanical Engineering, King Abdulaziz University, Jeddah, Saudi Arabia, P.O. Box #80204

Abstract

We needlessly squander heat energy through inefficient energy handling systems and usually this energy is low grade, whose recovery is generally futile. To this end, the thermoelectric field is a promising technology to directly transform some of this waste thermal energy back to electricity through the Seebeck effect. Among variety of thermoelectric materials, nanostructures and their heterostructures are the most auspicious for commercial applications due to their remarkably good thermoelectric performances. Although, the incorporation of metal telluride nanostructures and their heterostructures in thermoelectric devices has shown high performances, it is still questionable if such materials can be produced in scalable, reliable, and economical ways. Thus, this article is devoted to furnish the important breakthroughs in the metal telluride thermoelectrics during the last few decades.

Keywords: thermoelectricity; metal tellurides; nanostructures

1. Introduction

During the last few decades, there has been an urgent need for the clean and alternative renewable energy resources, because of environment destruction, global warming and energy crisis caused by our strong reliance on nonrenewable energy sources. Thermoelectric (TE) materials have engaged a substantial research not only due to their propitious efficacy in boosting energy conversion efficiency, in solid-state cooling and sensors [1–5], but also due to their potential advantages like, miniaturization, inexpensive, lightweight, noise and pollution free devices. Thermoelectric energy harvesting includes thermoelectric materials, devices and their applications in thermoelectric generators, refrigerators, automotive waste-heat recovery and in military systems. Thermoelectric effect is based on the fundamental interplay between the electronic and thermal properties

of a material. The two predominant thermoelectric effects are the Seebeck effect and the Peltier effect. When a thermal gradient is applied across an electrically conductive material, charge carriers drift along the gradient from high to low temperature; this is the so-called Seebeck effect. On the contrary, when an electric current is made to flow through a junction between two conductors, heat is generated or removed at the junction; this is the Peltier effect. Thermoelectric generators can be of immense application to convert waste heat into electricity by employing the Seebeck effect [6,7]. Meanwhile, thermoelectric refrigerators employing the Peltier effect could potentially replace compressor-based refrigerators avoiding the use of hydrochloroflourocarbon refrigerant [6,7]. The efficiency of these devices crucially depends on the properties of the materials employed. The optimization of these devices generated a dimensionless parameter, ZT , called figure of merit, which is used to determine the performance of a thermoelectric material. The figure of merit is given by

$$ZT = \frac{S^2 \sigma}{\kappa} T \quad (1)$$

where S is the Seebeck coefficient, σ is electrical conductivity, $\kappa = \kappa_L + \kappa_C$ is the thermal conductivity including the lattice thermal conductivity, κ_L , and the carrier thermal conductivity, κ_C , and T is absolute temperature [8]. The power factor ($S^2 \sigma$) is a critical quantity to compare electrical properties of thermoelectric materials.

Recently, a number of research papers have been published to improve the figure of merit (ZT) of thermoelectric materials [9–15]. TE materials have been successfully employed in electric water pump, climate control seat and TE generator of BMW series cars [16]. They are also the primary material in the radioisotope TE generators which supply electrical power to the Cassini spacecraft [17]. TE devices have recently found their possible application in lithium-ion batteries [18] and dye-sensitized solar cells [19]. However, such type

of applications require TE materials with higher ZT , which in turn calls for higher Seebeck coefficient, higher electrical conductivity and lower thermal conductivity. Moreover, the lower efficiency of TE materials also forbids their wide applications. Till now, a number of materials have been identified that have superior ZT value and lower cost for potential industrial applications [20–24].

2. Thermoelectric materials

The leading material for thermoelectric applications in commercial devices is bismuth telluride (Bi_2Te_3) with $ZT \sim 1$. It is a semiconductor with an indirect band gap of about 0.15 eV [25]. For producing p-type material it can be doped with Sb and with Se for n-type material. The atomic structure of Bi_2Te_3 consists of five layers of atoms $\text{Te}^{[1]} - \text{Bi} - \text{Te}^{[2]} - \text{Bi} - \text{Te}^{[1]}$, which is repeated. The layers are bound together by van der Waals interactions and owing to this factor Bi_2Te_3 crystals can be easily ripped along the layers. In context of the thermoelectrical properties, the Seebeck coefficient of doped Bi_2Te_3 is independent of orientation while Seebeck coefficient of undoped Bi_2Te_3 depends on the direction of the temperature gradient [26]. Recently, nanostructuring of Bi_2Te_3 has enhanced its ZT value. Sootsman et al. reported a record ZT value of 2.4 for superlattice of Bi_2Te_3 and Sb_2Te_3 at room temperature, grown by low-temperature metal-organic chemical vapour deposition technique. The high ZT value was obtained in the direction perpendicular to Bi_2Te_3 layers.

The leading method to enhance ZT in the 1960s was to control doping and form solid solutions such as $\text{Bi}_2\text{Te}_3 - \text{Sb}_2\text{Te}_3$, $\text{PbTe} - \text{SnTe}$. However, point defects in solid solutions decreases the lattice thermal conductivity by increasing heat carrying phonons scattering and also reduces charge carrier mobility, thus the ZT improvement by this method is limited [27]. From 1960-1990, there were no significant developments in thermoelectrics field and $(\text{Bi}_{1-x}\text{Sb}_x)_2(\text{Se}_{1-y}\text{Te}_y)_3$ alloy family remained the key commercial material with ZT of about 1 [2]. During the last two decades, thermoelectric community started exploring the next generation thermoelectric materials on the basis of the following two criteria: one is exploiting families of bulk thermoelectric materials with complex crystal structures, and the other is employing low-dimensional thermoelectric materials systems obtained via nanostructural engineering. An appreciable enhancement in ZT has been witnessed in the PGEC materials, and nanostructured materials, such as superlattices, quantum dots, nanowires, and nanocomposites.

2.1 Nanostructured thermoelectric materials

Hicks et al. proposed that it may be possible to increase ZT of certain materials by preparing them in quantum-well superlattice structures, since quantum confinement in the interlayer direction can increase the DOS near the Fermi level [28]. Their calculation showed that layering can enhance the figure of merit of a highly anisotropic material such as Bi_2Te_3 with the proviso that superlattice multilayers are designed in a particular orientation. They also suggested that the interfaces between layers would effectively scatter phonons if the Bi_2Te_3 layer thickness will be less than the phonon mfp, which will ultimately result in the decrease of lattice thermal conductivity [28,29]. Venkatasubramanian et al. [30] reported a significant enhancement in ZT (~ 2.4) employing $\text{Bi}_2\text{Te}_3 - \text{Sb}_2\text{Te}_3$ p-type quantum well superlattices with a periodicity of 6 nm, while the highest ZT value for the bulk Bi_2Te_3 alloy is only $ZT = 1.1$. Later on, Harman et al [31] synthesized quantum-dot super lattices in the $\text{PbTe} - \text{PbSeTe}$ system, wherein PbSe nanodots were embedded in a PbTe matrix, and reported $ZT = 1.6$, which is considerably higher than their bulk counterparts ($ZT = 0.34$). In addition, improved thermoelectric properties have also been reported for two-dimensional thin films and quantum well structures including Bi_2Te_3 superlattice-based thin-film [32], $\text{PbTe}/\text{Ag}_2\text{Te}$ thin films [33], quantum well/barrier $\text{PbTe}/\text{Pb}_{1-x}\text{Eu}_x\text{Te}$ structures [34], n - $\text{PbTe}/\text{pSnTe}/\text{n} - \text{PbTe}$ quantum wells [35].

The motive behind these investigations was the conjecture that the quantum confinement of in-plane carrier transport could significantly enhance the power factor over that of homogeneous materials that can lead to ten-fold increase in ZT . In this context, Shakouri [36] proposed that such enhancement can happen because the sharp features in the DOS of quantum-confined structures allows a doping-level-tuneable increase in the asymmetry between hot and cold electron transport. This subsequently leads to a large number of carriers moving in the material, thereby imparting a large Seebeck coefficient and higher electrical conductivity [37].

It has been found theoretically and experimentally that the low-dimensional nanostructured thermoelectric materials have higher ZT (> 3), since the density of states (DOS) near Fermi level can be enhanced through quantum confinement leading to an increase in thermopower. Moreover, phonons in these materials can be effectively scattered by high density of interfaces over a large mean free path (mfp) range, ensuing a decrease in the lattice thermal conductivity [38]. The TE properties of the nanostructured materials depend on the size and morphology of the microstructural features,

thus microstructural engineering should be focused in the development of TE nanomaterials. Saleemi et al. synthesized bulk nanostructured (NS) undoped Bi_2Te_3 via a promising chemical synthetic route [39]. They employed spark plasma sintering for compaction and sintering of the Bi_2Te_3 nanopowders. The average grain size of the final compacts was found to be 90 ± 5 nm. An enhanced ZT for the bulk undoped Bi_2Te_3 is obtained with a peak value of ~ 1.1 at 340 K.

Later on, a variety of Bi_2Te_3 -based compounds possessing different morphologies have been successfully synthesized by various research groups. These morphologies include nanowires [40], nanotubes [41], nanoplates and self-assembled nanoflowers [42], and nanobelts [43] via hydrothermal method [21] with ethylenediamine tetraacetic acid (EDTA) as an additive. However, ZT values of these structures after fortification with SPS are only about 0.7 [80, 83] but dense nanostructures can impart greatly enhanced phonon scattering, and therefore the thermal conductivity can be dramatically decreased to lower values.

Microstructural tailoring can be carried out to produce anisotropic polycrystalline, hierarchical nanostructure and nanocomposites via various techniques of synthesis and sintering process like hot-press or SPS. Recently, Jiang et al. synthesized nanostructured p-type $\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$ alloys with preferred orientation via the densification of nanostructured powders followed by a two-step hot forging process [45].

The nanopowders sintered for 20 minutes at 330 °C, produced samples with a density of 96% and the particle size was in nanometer range (50-300 nm, while that sintered at 450 °C for 5 minutes produced samples with randomly oriented flake-like grains with a density of 99% and size of several microns. The nanosized grains became elongated micro-sized flakes being well arranged perpendicular to the direction of the applied pressure.

Nanostructured thermoelectric materials can also be fabricated by introducing nanometer-sized polycrystallines and interfaces into the bulk materials; this inclusion can decrease the thermal conductivity by enhancing the phonon scattering. Since the phonon mfp generally ranges from several to a few hundred nanometres, while the carrier mfp is typically only a few nanometres, there is a high probability of preferential phonon scattering [46]. A variety of nanostructure composites have been fabricated by incorporating nanometer-sized polycrystallines (grain size ~ 5 nm–10 μm) via hot pressing or spark plasma sintering (SPS) of fine powders formed by grinding and milling or wet chemistry processing [38]. The nanocomposites produced by this method possess multitude of advantages over conventional fabrication techniques that generate very large-grain or single

crystal material, such as reduced thermal conductivity owing to phonon scattering at grain boundaries, improved mechanical properties and isotropy [37]. Bi_2Te_3 nanocomposites are outstanding thermoelectric materials at room temperature and are widely employed for commercial Peltier elements. Poudel et al. fabricated a polycrystalline p-type $\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$ bulk nanocomposite by hot pressing nanopowders that were ball-milled from crystalline ingots under inert conditions [47]. They reported a peak ZT of 1.2 at room temperature and ZT of 1.4 at 373 K, and thermal conductivity reduction from $1.3 \text{ W m}^{-1}\text{K}^{-1}$ in the bulk ingots to $1.0 \text{ W m}^{-1}\text{K}^{-1}$ in the nanocomposite form. However, the electrical conductivity of the nanocomposite was found to be reduced slightly due to which the maximum ZT of the nanocomposite was only 30% higher than the bulk ingots. The transmission electron microscopy (TEM) images revealed complex polygonal grain structures, with diameters ranging from few nanometers to few microns. Furthermore, the microstructure characterization showed Sb-rich nanodots ranging from 2 to 10 nm in diameter having diffused boundaries and pure Te precipitates with diameter between 5 to 30 nm. Poudel et al. proposed that these nanostructures could efficiently scatter larger wavelength phonons at the grain boundaries which might have imparted enhanced thermoelectric properties to Bi_2Te_3 -based nanocomposites [47]. Further researches unravelled that various other p-type Bi_2Te_3 -based nanocomposites can also achieve a high ZT , around 1.3 between 75 and 373 K [48] and 1.4 at 373 K [49], whereas n-type Bi_2Te_3 -based nanocomposite can approach a ZT of 1.04 at 398 K [50]. A relatively surpassing ZT of around 2.2 was attained with complex nanostructured PbTe-based alloy $\text{AgPb}_m\text{SbTe}_{2+m}$ (abbreviated as LAST) fabricated by the melt-grown method [51]. LAST alloys comprises of Ag–Sb rich nanoscale inclusions in the nanostructured matrix; these nanoscale inclusions played a critical role in reducing the thermal conductivity to about $2.3 \text{ W m}^{-1}\text{K}^{-1}$ at room temperature. A variety of other PbTe-based nanostructured thermoelectric materials have been developed including $\text{AgPb}_m\text{Sn}_n\text{SbTe}_{2+m+n}$ (LASTT), $\text{NaPb}_m\text{SbTe}_{2+m}$ (SALT-m), $\text{KPb}_m\text{SbTe}_{m+2}$ (PLAT-m) and $\text{PbTe} - \text{PbS}$, that achieved ZT values higher than 1 [52–68]. Androulakis et al. [55] demonstrated that certain compositions in $\text{Ag}(\text{Pb}_{1-y}\text{Sn}_y)_m\text{SbTe}_{2+m}$ series display high performance p-type thermoelectric properties owing to their very low thermal conductivity; for instance $ZT \sim 1.45$ at 630 K. They also showed that these materials are actually bulk nanocomposites and illustrated that properties such as carrier concentration, TE power, and thermal conductivity can be carefully tuned by varying the m and y values, as well as the Ag and Sb concentrations.

Another providential category of nanostructures are the nanotubes possessing high ZT values owing to their structural features such as low dimensionality and hollow tubular morphology [116, 117]. The V-VI nanotubes have been successfully prepared by the pulsed electrodeposition and the solution-phase method [5]. The pulsed electrodeposition method comprises of the fabrication of a porous anodic alumina (PAA) template with a meshlike Au layer, however, hitherto only Bi, Sb, Bi_2Te_3 and their derived ternary alloy nanotubes can be fabricated through this procedure [71–73]. Furthermore, the diameter, thickness, and crystallinity of the produced nanotubes cannot be precisely controlled with this method which can be a hurdle in achieving superior thermoelectric materials. In contrast, the solution-phase method has also been employed to prepare V-VI-based nanotubular structures, such as Bi, Bi_2Se_3 and Bi_2Te_3 nanotubes being synthesized through hydrothermal and galvanic replacement-reaction processes [74–77]. Nevertheless, these solution-phase methods have their own shortcomings, such as low production yields, crudely controlled size, and polycrystalline products. Zhang et al. [78] successfully synthesized highly crystalline Bi_2Te_3 nanotubes employing Te nanowires as the templates via ethylene glycol mediated solution phase method. The produced nanotubes were uniform and single crystalline with diameter and wall thickness of around 70 and 10–15 nm, respectively.

2.2 Heterostructures of Metal Telluride

It has been confirmed that the ZT of one-dimensional heterostructures of metal tellurides surpasses the ZT of other types of nanostructures, for instance conventional nanowires and nanoparticles [28,70,79,80]. Thus, during the last few years, fabrication of one-dimensional metal telluride heterostructures has become a research motif of paramount importance, owing to their practical applications as thermoelectric materials [81–83]. In comparison to conventional nanowires, the heterostructure interface between every two adjacent segments in a multisegmented nanowire or between the core and shell in a core/shell nanowire can decrease the lattice thermal conductivity by confining the phonon scattering along the wire axis [5,28,70,79,80]. Consequently, the current juncture calls for adroit and uncomplicated ways for synthesizing high-quality heterostructured nanowires in order to fabricate high performance thermoelectric devices.

A variety of V-VI based heterostructured nanowires have been produced via different chemical routes, including electrodeposition and solution-phase epitaxial growth. In particular, Bi/Sb, Bi/ $\text{Bi}_{0.5}\text{Sb}_{0.5}$, Bi_2Te_3 /Sb and $\text{Bi}_2\text{Te}_3/(\text{Bi}_{0.3}\text{Sb}_{0.7})_2\text{Te}_3$ multisegmented nanowires have been fabricated employing pulsed

electrodeposition in porous membrane templates [5,84–87]. It was found that the thermoelectric performance intensely depends upon the length of each segment, which can be well governed by varying the deposition time, deposition potential, and/or ion concentration in the electrolyte [5]. Bi_2Te_3 has been regarded among V-VI alloys as the leading thermoelectric material at room temperature [88].

Nevertheless, the Bi_2Te_3 -based multisegmented nanowires that were reported previously were polycrystalline, which may reduce the electrical conductivity and diminish the ZT value. Thus, there was a dire need to develop and fabricate Bi_2Te_3 -based multisegmented nanowires with a single-crystal structure. To this end, Wang et al. [89], synthesized $\text{Bi}_2\text{Te}_3/\text{Te}$ multiple heterostructure single-crystalline nanowire arrays via a facile thermal annealing process of the supersaturated Bi – Te alloy nanowire arrays. It was found that the precipitation confined by porous anodic alumina (PAA) membranes resulted in the spontaneous formation of the block-by-block structure. Furthermore, an intriguing result was unveiled promulgating that the length of each segment is dependent on the x value in the supersaturated $\text{Bi}_x\text{Te}_{1-x}$ nanowires; these segment length can be subtly controlled by varying the x composition.

There are few other techniques that can be found in literature for synthesizing Bi_2Te_3 nanowire heterostructures, although they require templates [87,89], complex surfactants [90], or catalysts [91] for the synthesis. More recently, Zhang et al. [92] explored the synthesis of 1D thermoelectric nanowire heterostructures fabricated via solution-phase chemical methods, specifically focusing on telluride-based compounds. They demonstrated a catalyst-free synthesis of Te – Bi_2Te_3 “barbell” nanowire heterostructures exhibiting strait diameter and length distribution. They were also able to almost control the density of the hexagonal Bi_2Te_3 plates fixed on the Te nanowires by changing the reaction conditions. Furthermore, they also synthesized other telluride-based compositionally transmuted nanowire heterostructures such as $\text{PbTe} - \text{Bi}_2\text{Te}_3$. The bulk pellets fabricated from Te – Bi_2Te_3 heterostructures exhibited a significant enhancement in the Seebeck coefficient and highly decreased thermal conductivity, which result in large figure of merit.

The synthesis steps in the fabrication of Te – Bi_2Te_3 nanowire heterostructures include growth of Te nanowires and then growth of two Bi_2Te_3 plates at the ends of Te nanowire by adding Bi precursor. The further characterization of intermediate product, Te nanowires, and the final product Te – Bi_2Te_3 “barbell” nanowire heterostructures, with X-ray powder diffraction (XRD) revealed pure hexagonal phase of Te (JCPDS No. 36-1452) and partial formation of Bi_2Te_3 (JCPDS No. 15-0863) after adding the Bi precursor.

3. Conclusion and Outlook

During the last two decades, research on thermoelectric materials has gained an unprecedented momentum, ultimately, boosting the figure of merit (ZT) of the materials from ~ 1 to 2.2–2.4 by nanostructure engineering. It is now established that the thermoelectric properties of metal tellurides can be improved through microstructural tailoring of their nanostructures, which leads to the decreased thermal conductivity by the selective scattering of phonons at the grain boundaries and amplified Seebeck coefficient by altering the density of states (DOS). It has been demonstrated that telluride nanowires and nanowire heterostructures can be easily synthesized in solution, which is an alternate method to fabricate bulk thermoelectric nanocomposites [92]. The reinforced pellets from nanowires and nanowire heterostructures exhibits exceptionally low thermal conductivities that results in superior thermoelectric properties. Furthermore, nanowires and nanowire heterostructures can be future paradigms for investigations such as energy filtering and modulation doping. Undoubtedly, these nanostructured materials and their heterostructures have opened new avenues for further research in thermoelectric materials.

Hitherto, attaining ZT values of 3 or more appears to be a strenuous task, which will require further cutback of thermal conductivity while simultaneously escalating electronic conduction. However, reduction in thermal conductivity below the amorphous limit will call for the alteration in the group velocity or decreasing the number of phonon modes that propagate. This can be achieved by coherent or correlated scattering effects, but thus far it has been proved to be insurmountable task for the phonons, and thermal conductivity reduction via such techniques has never been illustrated by researchers. This notion thus put forth an open challenge to the theorists and experimentalists to conceive neoteric scattering mechanisms and concepts that will further reduce the thermal conductivity.

Since, the microstructure morphology of TE materials governs the transport properties, controlled microstructural tailoring of grain size and shape is advantageous to obtain higher ZT values. Thus there is a dire need to comprehend phase diagrams and related defect theory and assess the effect of defects on the transport properties of TE materials. More investigations should be focused on synthesizing nanostructured particles at a large scale and cheap price, which will ultimately result in commercial applications of TE materials.

Moreover, the thermoelectric properties seems to be crucially influenced by the nanostructure, synthesis approach and device assembly. Thus, researchers should focus on thermoelectric nanomaterials with narrow

bandgaps, heavy elements doping, point defects loading and nanostructuring [38]. For realistic thermoelectric applications, the synthesis techniques for thermoelectric materials should be scalable, have superior quality and cheap. The nanostructured materials must be in compact form so as to aid machining and the nanoscale characteristics should possess high thermal stability at longer time scales.

The high-performance shape-engineerable thermoelectric painting has also been a novel innovation in thermoelectric technology, wherein the painting is demonstrated to be geometrically compatible to surfaces of any shape [93]. The inorganic paint was based on Bi_2Te_3 and the molecular Sb_2Te_3 chalcogenidometalate as a sintering agent for thermoelectric particles. The ZT values was found to be 0.67 for n-type and 1.21 for p-type painted materials which are well in comparison with their bulk counterpart.

References:

- [1] L.E. Bell, Cooling, heating, generating power, and recovering waste heat with thermoelectric systems., *Science*. 321 (2008) 1457–1461. doi:10.1126/science.1158899.
- [2] M.S. Dresselhaus, G. Chen, M.Y. Tang, R. Yang, H. Lee, D. Wang, Z. Ren, J.P. Fleurial, P. Gogna, New directions for low-dimensional thermoelectric materials, *Adv. Mater.* 19 (2007) 1043–1053. doi:10.1002/adma.200600527.
- [3] B.C. Sales, THERMOELECTRIC MATERIALS: Smaller Is Cooler, *Science* (80-). 295 (2002) 1248–1249. doi:10.1126/science.1069895.
- [4] G.J. Snyder, E.S. Toberer, Complex thermoelectric materials, *Nat. Mater.* 7 (2008) 105–114. doi:10.1038/nmat2090.
- [5] G. Zhang, Q. Yu, W. Wang, X. Li, Nanostructures for thermoelectric applications: Synthesis, growth mechanism, and property studies, *Adv. Mater.* 22 (2010) 1959–1962. doi:10.1002/adma.200903812.
- [6] A.F. Joffe, The Revival of Thermoelectricity, *Sci. Am.* 199 (1958) 31–37. doi:10.1038/scientificamerican1158-31.
- [7] G.J. Snyder, Small thermoelectric generators., *Electrochem. Soc. Interface.* 17 (2008) 54–56. doi:10.1109/ICT.2002.1190351.
- [8] H.J. Goldsmid, Introduction to Thermoelectricity, Springer, Heidelberg, Germany, 2010.
- [9] J.R. Szczech, J.M. Higgins, S. Jin, Enhancement of the thermoelectric properties in nanoscale and nanostructured materials, *J. Mater. Chem.* 21 (2011) 4037–4055.

- doi:10.1039/C0JM02755C.
- [10] L.D. Hicks, T.C. Harman, X. Sun, M.S. Dresselhaus, Experimental study of the effect of quantum-well structures on the thermoelectric figure of merit, *Phys. Rev. B (Condensed Matter)*. 53 (1996) 10493–10496. doi:10.1103/PhysRevB.53.R10493.
- [11] C. Candolfi, U. Aydemir, A. Ormeci, M. Baitinger, N. Oeschler, F. Steglich, Y. Grin, Low-temperature magnetic, galvanomagnetic, and thermoelectric properties of the type-I clathrates Ba₈Ni_xSi_{46-x}, *Phys. Rev. B - Condens. Matter Mater. Phys.* 83 (2011). doi:10.1103/PhysRevB.83.205102.
- [12] P. Vaqueiro, A. V. Powell, Recent developments in nanostructured materials for high-performance thermoelectrics, *J. Mater. Chem.* 20 (2010) 9577–9584. doi:10.1039/c0jm01193b.
- [13] K.F. Hsu, S. Loo, F. Guo, W. Chen, J.S. Dyck, Bulk Thermoelectric Materials with High Figure of Merit, *Science (80-.)*. 303 (2004) 818–821. doi:10.1126/science.1092963.
- [14] B.C. Sales, Critical overview of recent approaches to improved thermoelectric materials, *Int. J. Appl. Ceram. Technol.* 4 (2007) 291–296. doi:10.1111/j.1744-7402.2007.02143.x.
- [15] P. Pichanusakorn, P.R. Bandaru, Minimum length scales for enhancement of the power factor in thermoelectric nanostructures, *J. Appl. Phys.* 107 (2010). doi:10.1063/1.3359659.
- [16] W. He, G. Zhang, X. Zhang, J. Ji, G. Li, X. Zhao, Recent development and application of thermoelectric generator and cooler, *Appl. Energy*. 143 (2015) 1–25. doi:10.1016/j.apenergy.2014.12.075.
- [17] M. V. Frank, Probabilistic analysis of the inadvertent reentry of the Cassini spacecraft's radioisotope thermoelectric generators, *Risk Anal.* 20 (2000) 251–260. doi:10.1111/0272-4332.202024.
- [18] Y. Liu, S. Yang, B. Guo, C. Deng, G. Lauriat, Numerical Analysis and Design of Thermal Management System for Lithium Ion Battery Pack Using Thermoelectric Coolers, *Adv. Mech. Eng.* 2014 (2014) 1–8. doi:http://dx.doi.org/10.1155/2014/852712.
- [19] S. Su, T. Liu, Y. Wang, X. Chen, J. Wang, J. Chen, Performance optimization analyses and parametric design criteria of a dye-sensitized solar cell thermoelectric hybrid device, *Appl. Energy*. 120 (2014) 16–22. doi:10.1016/j.apenergy.2014.01.048.
- [20] W. Xie, A. Weidenkaff, X. Tang, Q. Zhang, J. Poon, T. Tritt, Recent advances in nanostructured thermoelectric Half-Heusler compounds, *Nanomaterials*. 2 (2012) 379–412. doi:10.3390/nano2040379.
- [21] Q. Jiang, J. Yang, Y. Liu, H. He, Microstructure tailoring in nanostructured thermoelectric materials, *J. Adv. Dielectr.* 6 (2016) 1630002. doi:10.1142/S2010135X16300024.
- [22] C. Wan, Y. Wang, N. Wang, W. Norimatsu, M. Kusunoki, K. Koumoto, Development of novel thermoelectric materials by reduction of lattice thermal conductivity, *Sci. Technol. Adv. Mater.* 11 (2010) 7. doi:10.1088/1468-6996/11/4/044306.
- [23] L.-D. Zhao, J. He, D. Berardan, Y. Lin, J.-F. Li, C. Nan, N. Dragoe, BiCuSeO oxyselenides: new promising thermoelectric materials, *Energy Environ. Sci.* 7 (2014) 2900–2924. doi:10.1039/c4ee00997e.
- [24] J.-F. Li, W.-S. Liu, L.-D. Zhao, M. Zhou, High-performance nanostructured thermoelectric materials, *NPG Asia Mater.* 2 (2010) 152–158. doi:10.1038/asiamat.2010.138.
- [25] J.R. Sootsman, D.Y. Chung, M.G. Kanatzidis, New and old concepts in thermoelectric materials, *Angew. Chemie - Int. Ed.* 48 (2009) 8616–8639. doi:10.1002/anie.200900598.
- [26] G.S. Nolas, J. Sharp, H.J. Goldsmid, *Thermoelectrics : basic principles and new materials developments.*, Springer, Berlin, London, 2001.
- [27] S.K. Bux, J.P. Fleurial, R.B. Kaner, Nanostructured materials for thermoelectric applications., *Chem. Commun. (Camb)*. 46 (2010) 8311–24. doi:10.1039/c0cc02627a.
- [28] L.D. Hicks, M.S. Dresselhaus, Effect of quantum-well structures on the thermoelectric figure of merit, *Phys. Rev.* 47 (1993) 12727–12731.
- [29] L.D. Hicks, T.C. Harman, M.S. Dresselhaus, Use of quantum-well superlattices to obtain a high figure of merit from nonconventional thermoelectric materials, *Appl. Phys. Lett.* 63 (1993) 3230–3232. doi:10.1063/1.110207.
- [30] R. Venkatasubramanian, E. Siivola, T. Colpitts, B. O'Quinn, Thin-film thermoelectric devices with high room-temperature figures of merit., *Nature*. 413 (2001) 597–602. doi:10.1038/35098012.
- [31] T.C. Harman, P.J. Taylor, M.P. Walsh, B.E. Laforge, Quantum Dot Superlattice Thermoelectric Materials and Devices, *Science (80-.)*. 2229 (2008). doi:10.1126/science.1072886.
- [32] I. Chowdhury, R. Prasher, K. Lofgreen, G.

- Chrysler, S. Narasimhan, R. Mahajan, D. Koester, R. Alley, R. Venkatasubramanian, On-chip cooling by superlattice-based thin-film thermoelectrics, *Nat. Nanotechnol.* 4 (2009) 235–238. doi:10.1038/nano.2008.417.
- [33] J.J. Urban, D. V Talapin, E. V Shevchenko, C.R. Kagan, C.B. Murray, Synergism in binary nanocrystal superlattices leads to enhanced p-type conductivity in self-assembled PbTe/Ag₂Te thin films., *Nat. Mater.* 6 (2007) 115–121. doi:10.1038/nmat1826.
- [34] L.D. Hicks, T.C. Harman, X. Sun, M.S. Dresselhaus, Experimental study of the effect of quantum-well structures on the thermoelectric figure of merit, *Phys. Rev. B.* 53 (1996) R10493–R10496. Z:\Articles\superlattices-inplane\Hicks-PRB-1996.pdf.
- [35] E.I. Rogacheva, O.N. Nashchekina, A. V. Meriuts, S.G. Lyubchenko, M.S. Dresselhaus, G. Dresselhaus, Quantum size effects in n-PbTe/p-SnTe/n-PbTe heterostructures, *Appl. Phys. Lett.* 86 (2005) 1–3. doi:10.1063/1.1862338.
- [36] A. Shakouri, Thermoelectric, thermionic and thermophotovoltaic energy conversion, *Int. Conf. Thermoelectr. ICT, Proc. 2005* (2005) 495–500. doi:10.1109/ICT.2005.1519994.
- [37] C.J. Vineis, A. Shakouri, A. Majumdar, M.G. Kanatzidis, Nanostructured thermoelectrics: Big efficiency gains from small features, *Adv. Mater.* 22 (2010) 3970–3980. doi:10.1002/adma.201000839.
- [38] Z.G. Chen, G. Han, L. Yang, L. Cheng, J. Zou, Nanostructured thermoelectric materials: Current research and future challenge, *Prog. Nat. Sci. Mater. Int.* 22 (2012) 535–549. doi:10.1016/j.pnsc.2012.11.011.
- [39] M. Saleemi, M.S. Toprak, S. Li, M. Johnsson, M. Muhammed, Synthesis, processing, and thermoelectric properties of bulk nanostructured bismuth telluride (Bi₂Te₃), *J. Mater. Chem.* 22 (2012) 725. doi:10.1039/c1jm13880d.
- [40] H. Yang, S.W. Finefrock, J.D. Albarracin Caballero, Y. Wu, Environmentally benign synthesis of ultrathin metal telluride nanowires, *J. Am. Chem. Soc.* 136 (2014) 10242–10245. doi:10.1021/ja505304v.
- [41] H.-T. Zhu, J. Luo, J.-K. Liang, Synthesis of highly crystalline Bi₂Te₃ nanotubes and their enhanced thermoelectric properties, *J. Mater. Chem. A.* 2 (2014) 12821–12826. doi:10.1039/C4TA02532F.
- [42] J. Fu, S. Song, X. Zhang, F. Cao, L. Zhou, X. Li, H. Zhang, Bi₂Te₃ nanoplates and nanoflowers: Synthesized by hydrothermal process and their enhanced thermoelectric properties, *CrystEngComm.* 14 (2012) 2159–2165. doi:10.1039/c2ce06348d.
- [43] W. Shi, J. Yu, H. Wang, H. Zhang, Hydrothermal synthesis of single-crystalline antimony telluride nanobelts, *J. Am. Chem. Soc.* 128 (2006) 16490–16491. doi:10.1021/ja066944r.
- [44] S.W. Finefrock, G. Zhang, J.H. Bahk, H. Fang, H. Yang, A. Shakouri, Y. Wu, Structure and thermoelectric properties of spark plasma sintered ultrathin PbTe nanowires, *Nano Lett.* 14 (2014) 3466–3473. doi:10.1021/nl500997w.
- [45] Q. Jiang, H. Yan, J. Khaliq, H. Ning, S. Grasso, K. Simpson, M.J. Reece, Large ZT enhancement in hot forged nanostructured p-type Bi_{0.5}Sb_{1.5}Te₃ bulk alloys, *J. Mater. Chem. A.* 2 (2014) 5785–5790. doi:10.1039/C3TA13952B.
- [46] J.R. Szczech J.M. Higgins, S. Jin, Enhancement of the thermoelectric properties in nanoscale and nanostructured materials, *J. Mater. Chem.* 21 (2011) 4037–4055. doi:10.1039/c0jm02755c.
- [47] B. Poudel, Q. Hao, Y. Ma, Y. Lan, A. Minnich, B. Yu, X. Yan, D. Wang, A. Muto, D. Vashaee, X. Chen, J. Liu, M.S. Dresselhaus, G. Chen, Z. Ren, High-thermoelectric performance of nanostructured bismuth antimony telluride bulk alloys., *Science.* 320 (2008) 634–8. doi:10.1126/science.1156446.
- [48] Y. Ma, Q. Hao, B. Poudel, Y. Lan, B. Yu, D. Wang, G. Chen, Z. Ren, Enhanced thermoelectric figure-of-merit in p-type nanostructured bismuth antimony tellurium alloys made from elemental chunks, *Nano Lett.* 8 (2008) 2580–2584. doi:10.1021/nl8009928.
- [49] Y. Lan, B. Poudel, Y. Ma, D. Wang, M.S. Dresselhaus, G. Chen, Z. Ren, Structure study of bulk nanograined thermoelectric bismuth antimony telluride, *Nano Lett.* 9 (2009) 1419–1422. doi:10.1021/nl803235n.
- [50] X. Yan, B. Poudel, Y. Ma, W.S. Liu, G. Joshi, H. Wang, Y. Lan, D. Wang, G. Chen, Z.F. Ren, Experimental studies on anisotropic thermoelectric properties and structures of n-type Bi₂Te_{2.7}Se_{0.3}, *Nano Lett.* 10 (2010) 3373–3378. doi:10.1021/nl101156v.
- [51] K.F. Hsu, S. Loo, F. Guo, W. Chen, J.S. Dyck, C. Uher, T. Hogan, E.K. Polychroniadis, M.G. Kanatzidis, Cubic AgPbmSbTe_{2+m}: Bulk thermoelectric materials with high figure of merit, *Science* (80-.). 303 (2004) 818–821.
- [52] E. Quarez, K.F. Hsu, R. Pcionek, N. Frangis, E.K. Polychroniadis, M.G. Kanatzidis, Nanostructuring, compositional fluctuations, and atomic ordering in the thermoelectric

- materials AgPbmSbTe_{2+m}. The myth of solid solutions, *J. Am. Chem. Soc.* 127 (2005) 9177–9190. doi:10.1021/ja051653o.
- [53] P.F.P. Poudeu, J. D'Angelo, A.D. Downey, J.L. Short, T.P. Hogan, M.G. Kanatzidis, High thermoelectric figure of merit and nanostructuring in bulk p-type Na_{1-x}PbmSb_yTe_{m+2}, *Angew. Chemie - Int. Ed.* 45 (2006) 3835–3839. doi:10.1002/anie.200600865.
- [54] J. Androulakis, C.-H. Lin, H.-J. Kong, C. Uher, C.-I. Wu, T. Hogan, B.A. Cook, T. Caillat, K.M. Paraskevopoulos, M.G. Kanatzidis, Spinodal Decomposition and Nucleation and Growth as a Means to Bulk Nanostructured Thermoelectrics: Enhanced Performance in Pb_{1-x}Sn_xTe–PbS, *J. Am. Chem. Soc.* 129 (2007) 9780–9788. doi:10.1021/ja071875h.
- [55] J. Androulakis, K.F. Hsu, R. Pcionek, H. Kong, C. Uher, J.J. D'Angelo, A. Downey, T. Hogan, M.G. Kanatzidis, Nanostructuring and high thermoelectric efficiency in p-type Ag(Pb_{1-y}Sn_y)mSbTe_{2+m}, *Adv. Mater.* 18 (2006) 1170–1173. doi:10.1002/adma.200502770.
- [56] B. a Cook, M.J. Kramer, J.L. Haringa, M.K. Han, D.Y. Chung, M.G. Kanatzidis, Analysis of Nanostructuring in High Figure-of-Merit Ag_{1-x}PbmSbTe_{2+m} Thermoelectric Materials, *Adv. Funct. Mater.* 19 (2009) 1254–1259. doi:10.1002/adfm.200801284.
- [57] P.F.P. Poudeu, A. Guéguen, C.-I. Wu, T. Hogan, M.G. Kanatzidis, High Figure of Merit in Nanostructured n-Type KPbmSbTe_{m+2} Thermoelectric Materials†, *Chem. Mater.* 22 (2010) 1046–1053. doi:10.1021/cm902001c.
- [58] S.N. Girard, J. He, C. Li, S. Moses, G. Wang, C. Uher, V.P. Dravid, M.G. Kanatzidis, In situ nanostructure generation and evolution within a bulk thermoelectric material to reduce lattice thermal conductivity, *Nano Lett.* 10 (2010) 2825–2831. doi:10.1021/nl100743q.
- [59] J.R. Sootsman, H. Kong, C. Uher, J.J. D'Angelo, C.I. Wu, T.P. Hogan, T. Caillat, M.G. Kanatzidis, Large enhancements in the thermoelectric power factor of bulk PbTe at high temperature by synergistic nanostructuring, *Angew. Chemie - Int. Ed.* 47 (2008) 8618–8622. doi:10.1002/anie.200803934.
- [60] J.R. Sootsman, J. He, V.P. Dravid, S. Ballikaya, D. Vermeulen, C. Uher, M.G. Kanatzidis, Microstructure and thermoelectric properties of mechanically robust PbTe-Si eutectic composites, *Chem. Mater.* 22 (2010) 869–875. doi:10.1021/cm9016672.
- [61] J. He, S.N. Girard, M.G. Kanatzidis, V.P. Dravid, Microstructure-lattice thermal conductivity correlation in nanostructured PbTe_{0.7}Sn_{0.3} thermoelectric materials, *Adv. Funct. Mater.* 20 (2010) 764–772. doi:10.1002/adfm.200901905.
- [62] P.F.P. Poudeu, J. D'Angelo, H.J. Kong, A. Downey, J.L. Short, R. Pcionek, T.P. Hogan, C. Uher, M.G. Kanatzidis, Nanostructures versus solid solutions: Low lattice thermal conductivity and enhanced thermoelectric figure of merit in Pb_{9.6}Sb_{0.2}Te_{10-x}Sex bulk materials, *J. Am. Chem. Soc.* 128 (2006) 14347–14355. doi:10.1021/Ja0647811.
- [63] J. He, J.R. Sootsman, S.N. Girard, J.C. Zheng, J. Wen, Y. Zhu, M.G. Kanatzidis, V.P. Dravid, On the origin of increased phonon scattering in nanostructured pbte based thermoelectric materials, *J. Am. Chem. Soc.* 132 (2010) 8669–8675. doi:10.1021/ja1010948.
- [64] J.R. Sootsman, R.J. Pcionek, H. Kong, C. Uher, M.G. Kanatzidis, Strong reduction of thermal conductivity in nanostructured PbTe prepared by matrix encapsulation, *Chem. Mater.* 18 (2006) 4993–4995. doi:10.1021/cm0612090.
- [65] M.K. Han, K. Hoang, H. Kong, R. Pcionek, C. Uher, K.M. Paraskevopoulos, S.D. Mahanti, M.G. Kanatzidis, Substitution of Bi for Sb and its role in the thermoelectric properties and nanostructuring in Ag_{1-x}Pb₁₈MTe₂₀ (M = Bi, Sb) (x = 0, 0.14, 0.3), *Chem. Mater.* 20 (2008) 3512–3520. doi:10.1021/cm703661g.
- [66] P.F.P. Poudeu, C. Li, S. Moses, C. Uher, J. He, V. Dravid, K.M. Paraskevopoulos, M.G. Kanatzidis, Thermoelectric Properties and Nanostructuring in the p-Type Materials NaPb_{18-x}Sn_xMTe₂₀ (M=Sb, Bi), *Chem. Mater.* 20 (2009) 1683–1694.
- [67] K. Ahn, C.P. Li, C. Uher, M.G. Kanatzidis, Thermoelectric properties of the compounds AgPbmLaTe_{m+2}, *Chem. Mater.* 22 (2010) 876–882. doi:10.1021/cm901668h.
- [68] C.B. Lioutas, N. Frangis, I. Todorov, D.Y. Chung, M.G. Kanatzidis, Understanding nanostructures in thermoelectric materials: An electron microscopy study of AgPb₁₈Sb₂Se₂₀ crystals, *Chem. Mater.* 22 (2010) 5630–5635. doi:10.1021/cm102016j.
- [69] R. Prasher, W. Evans, P. Meakin, J. Fish, P. Phelan, P. Keblinski, Effect of aggregation on thermal conduction in colloidal nanofluids, *Appl. Phys. Lett.* 89 (2006). doi:10.1063/1.2360229.
- [70] R. Yang, G. Chen, M.S. Dresselhaus, Thermal conductivity modeling of core-shell and tubular nanowires, *Nano Lett.* 5 (2005) 1111–1115. doi:10.1021/nl0506498.
- [71] L. Li, Y.W. Yang, X.H. Huang, G.H. Li, R.

- Ang, L.D. Zhang, Fabrication and electronic transport properties of Bi nanotube arrays, *Appl. Phys. Lett.* 88 (2006). doi:10.1063/1.2184990.
- [72] D. Yang, G. Meng, Q. Xu, F. Han, M. Kong, L. Zhang, Electronic transport behavior of bismuth nanotubes with a predesigned wall thickness, *J. Phys. Chem. C.* 112 (2008) 8614–8616. doi:10.1021/jp8008892.
- [73] X.H. Li, B. Zhou, L. Pu, J.J. Zhu, Electrodeposition of Bi₂Te₃ and Bi₂Te₃ derived alloy nanotube arrays, *Cryst. Growth Des.* 8 (2008) 771–775. doi:10.1021/cg7006759.
- [74] Y. Li, J. Wang, Z. Deng, Y. Wu, Bismuth Nanotubes : A Rational Low-Temperature Synthetic Route, (2001) 9904–9905.
- [75] H. Cui, H. Liu, X. Li, J. Wang, F. Han, X. Zhang, R.I. Boughton, Synthesis of Bi₂Se₃ thermoelectric nanosheets and nanotubes through hydrothermal co-reduction method, *J. Solid State Chem.* 177 (2004) 4001–4006. doi:10.1016/j.jssc.2004.06.042.
- [76] X.B. Zhao, X.H. Ji, Y.H. Zhang, T.J. Zhu, J.P. Tu, X.B. Zhang, Bismuth telluride nanotubes and the effects on the thermoelectric properties of nanotube-containing nanocomposites, *Appl. Phys. Lett.* 86 (2005) 1–3. doi:10.1063/1.1863440.
- [77] F. Xiao, B. Yoo, K.H. Lee, N. V Myung, Synthesis of Bi₂Te₃ Nanotubes by Galvanic Displacement, *J. Am. Chem. Soc.* 129 (2007) 10068–10069. doi:10.1021/ja073032w.
- [78] G. Zhang, Q. Yu, Z. Yao, X. Li, Large scale highly crystalline Bi₂Te₃ nanotubes through solution phase nanoscale Kirkendall effect fabrication., *Chem. Commun. (Camb).* (2009) 2317–2319. doi:10.1039/b822595h.
- [79] Y.-M. Lin, M. Dresselhaus, Thermoelectric properties of superlattice nanowires, *Phys. Rev. B.* 68 (2003) 1–14. doi:10.1103/PhysRevB.68.075304.
- [80] L.D. Hicks, M.S. Dresselhaus, Thermoelectric figure of merit of a one-dimensional conductor, *Phys. Rev. B.* 47 (1993) 16631–16634. doi:10.1103/PhysRevB.47.16631.
- [81] C.M. Lieber, Z.L. Wang, Functional Nanowires, *MRS Bull.* 32 (2007) 99–108. doi:10.1557/mrs2007.41.
- [82] A.J. Mieszawska, R. Jalilian, G.U. Sumanasekera, F.P. Zamborini, The synthesis and fabrication of one-dimensional nanoscale heterojunctions, *Small.* 3 (2007) 722–756. doi:10.1002/smll.200600727.
- [83] Y. Wu, J. Xiang, C. Yang, W. Lu, C.M. Lieber, Single-crystal metallic nanowires and metal/semiconductor nanowire heterostructures., *Nature.* 430 (2004) 61–65. doi:10.1038/nature02811.
- [84] B. Yoo, F. Xiao, K.N. Bozhilov, J. Herman, M.A. Ryan, N. V. Myung, Electrodeposition of thermoelectric superlattice nanowires, *Adv. Mater.* 19 (2007) 296–299. doi:10.1002/adma.200600606.
- [85] F.H. Xue, G.T. Fei, B. Wu, P. Gui, L.D. Zhang, Direct electrodeposition of highly dense Bi/Sb superlattice nanowire arrays, *J. Am. Chem. Soc.* 127 (2005) 15348–15349. doi:10.1021/ja0547073.
- [86] X. Dou, G. Li, H. Lei, Kinetic versus thermodynamic control over growth process of electrodeposited Bi/BiSb superlattice nanowires, *Nano Lett.* 8 (2008) 1286–1290. doi:10.1021/nl073039b.
- [87] W. Wang, G. Zhang, X. Li, Manipulating growth of thermoelectric Bi₂Te₃/Sb multilayered nanowire arrays, *J. Phys. Chem. C.* 112 (2008) 15190–15194. doi:10.1021/jp803207r.
- [88] D.M. Rowe, *CRC Handbook of Thermoelectrics*, New York, 16 (1995) 1251–1256. doi:10.1016/S0960-1481(98)00512-6.
- [89] W. Wang, X. Lu, T. Zhang, G. Zhang, W. Jiang, X. Li, Bi₂Te₃/Te multiple heterostructure nanowire arrays formed by confined precipitation, *J. Am. Chem. Soc.* 129 (2007) 6702–6703. doi:10.1021/ja070976c.
- [90] W. Lu, Y. Ding, Y. Chen, Z.L. Wang, J. Fang, Bismuth telluride hexagonal nanoplatelets and their two-step epitaxial growth, *J. Am. Chem. Soc.* 127 (2005) 10112–10116. doi:10.1021/ja052286j.
- [91] W. Wang, J. Goebel, L. He, S. Aloni, Y. Hu, L. Zhen, Y. Yin, Epitaxial growth of shape-controlled Bi₂Te₃-Te heterogeneous nanostructures, *J. Am. Chem. Soc.* 132 (2010) 17316–17324. doi:10.1021/ja108186w.
- [92] G. Zhang, H. Fang, H. Yang, L.A. Jauregui, Y.P. Chen, Y. Wu, Design principle of telluride-based nanowire heterostructures for potential thermoelectric applications, *Nano Lett.* 12 (2012) 3627–3633. doi:10.1021/nl301327d.
- [93] S.H. Park, S. Jo, B. Kwon, F. Kim, H.W. Ban, J.E. Lee, D.H. Gu, S.H. Lee, Y. Hwang, J.-S. Kim, D.-B. Hyun, S. Lee, K.J. Choi, W. Jo, J.S. Son, High-performance shape-engineerable thermoelectric painting, *Nat. Commun.* 7 (2016) 13403. doi:10.1038/ncomms13403.